

Quantum Chemistry: An Understanding

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ABSTRACT

Since it influences the future development of quantum computers, precise estimation of quantum resources is crucial for expanding applications in quantum chemistry. A methodical methodology founded on a trustworthy metric is necessary to facilitate effective resource estimation. In this work, we present Quantum Resource Estimator (QRE), a Python software program that estimates the quantum resources required to compute molecular characteristics. Key specifications for the quantum phase estimation (QPE) algorithm across different chemical basis sets are defined by QRE. In particular, it determines the estimated time to solution, circuit depth, and number of ancilla qubits. Atom kinds, molecular geometries, charges, selected basis sets, and theoretical level are among the input data that QRE uses about molecules. It also incorporates an error analysis approach for identifying the required ancilla qubits using the QPE algorithm. For a single Trotter step, QRE calculates the number of rotation and CNOT gates as part of the estimation. Based on goal success probabilities, CNOT gate fidelities, and specified gate durations, the program then uses these computations to determine the total cost for entire QPE algorithms. The goal of this work is to advance knowledge of the present and future constraints of quantum computers in applications related to quantum chemistry.

Key Words: QRE, CNOT, Quantum

INTRODUCTION

A crucial and continuing research challenge is how many quantum resources—such as gate counts, circuit depth, and the amount of physical qubits—are required to fully utilize quantum computers for real-world applications. Understanding the resource requirements of different quantum algorithms becomes crucial as quantum computing technologies advance in order to close the gap between theoretical potential and practical use. The field of quantum chemistry, which aims to use quantum computers to address molecular problems, has a special set of difficulties that need for precise and methodical estimation of quantum resources.

It is essential to take a thorough and methodologically sound approach to addressing these issues. This entails carefully determining and examining the primary quantum resource indicators that affect the viability and performance of simulations of quantum chemistry. In addition to the number of quantum gates and circuit depth, which have an impact on runtime and computational complexity, these metrics also include the number of physical qubits needed to represent logical qubits and manage error correction, along with other elements like success probabilities, error rates, and gate fidelities. Other aspects of the system's chemical makeup, such as atom kinds, molecule geometries, charges, and basis sets, must also be taken into account in quantum chemistry.

In order to forecast the quantum resources needed to implement quantum algorithms for researching molecular characteristics, we created the Quantum Resource Estimator (QRE) program in this study. As a framework for resource estimate, the QRE software provides a thorough assessment of the quantum resources required to carry out quantum chemistry algorithms. The number of ancilla qubits (auxiliary qubits used for error correction), gate counts (which establish the number of quantum operations), circuit depth (the number of layers of gates needed), and runtime (the total amount of computation time) are among the resources that QRE can specifically estimate.

The QRE software combines computational characteristics like error rates, gate fidelities, and the intended target success probability with molecule-specific data, including the atomic structure, molecular geometries, charges, and the selected basis sets. Because of this integration, QRE is able to offer resource projections that are extremely precise and comprehensive, customized for the particular molecular system under simulation. By taking these things into account, QRE gives researchers a clear picture of the quantum resources needed to model chemical systems, especially on upcoming and near-term quantum computers that might still be constrained by a number of factors like coherence times, error rates, and qubit connectivity.

Furthermore, by elucidating the resource requirements of existing quantum technology, QRE provides important insights into the viability of quantum chemical applications. It assists in measuring the discrepancy between theoretical forecasts and real-world application, emphasizing the obstacles and constraints that need to be addressed in order to carry out high-precision molecular system simulations. Additionally, this tool helps lead future research towards maximizing resource utilization and minimizing errors in quantum computations, which in turn drives the creation of more efficient quantum algorithms and quantum structures.

By this work, we enable researchers create more effective quantum devices and algorithms by advancing our understanding of the possibilities and constraints of quantum chemical applications. Thus, the QRE program is a crucial step in bringing the practical use of quantum computers to the resolution of intricate chemical issues, with wide-ranging effects on domains from drug discovery to material research and beyond.

Literature Review on Quantum Resource Estimation in Quantum Chemistry

With the advent of quantum computer techniques, quantum chemistry simulations have advanced significantly and have the potential to completely change how we approach solving intricate chemical problems. As quantum computers develop further, calculating the quantum resources needed to run these simulations has emerged as a crucial research topic. Resource estimate for quantum chemistry applications has been the subject of numerous studies, with particular attention paid to quantum algorithms, gate counts, physical qubits, error correction, and computing time. The main advancements in quantum resource estimation are reviewed in this literature review, with particular attention paid to variational quantum eigensolvers (VQE), quantum phase estimation (QPE), and the difficulties in scaling quantum chemistry problems.

1. Quantum Phase Estimation (QPE) and Quantum Resource Estimation

One of the most crucial quantum techniques for resolving issues in quantum chemistry is quantum phase estimation (QPE). It is useful for estimating the Hamiltonian operator's eigenvalues, which are essential for figuring out the energy levels of molecules. Many studies have been conducted on the quantum resources needed to perform QPE. Aspuru-Guzik et al. (2005) demonstrated that QPE could effectively compute molecular energies with polynomial scaling by introducing a quantum approach for modeling molecular systems. However, accurate knowledge of the quantum resources required, such as the quantity of qubits and gate operations needed for accuracy, is necessary for practical implementation on quantum computers.

In the context of quantum chemistry, Chiesa et al. (2018) investigated the quantum resources needed for QPE, especially calculating the quantity of qubits and gates required to model electronic structure difficulties. They came to the conclusion that the number of qubits increases as the complexity of the molecular system increases, and that the quantum resource requirements for QPE scale dramatically with system size and precision. They also underlined how crucial error correction is to preserving the precision of quantum calculations as problem sizes grow.

2. Variational Quantum Eigensolver (VQE) and Quantum Resource Estimation

For quantum chemistry simulations, the Variational Quantum Eigensolver (VQE) has shown promise as a substitute for QPE, particularly for near-term quantum devices that might not yet be able to handle full-scale QPE. The electronic structure problem is resolved by VQE using parameterized quantum circuits and classical optimization. VQE was presented by Peruzzo et al. (2014), who also showed how it may be used for quantum chemical simulations on tiny quantum computers. The particular chemical system being studied and the ansatz that is selected have a significant impact on VQE's resource needs.

Estimating the quantum resources needed to perform VQE has been the subject of several studies. The resource scaling for the Unitary Coupled Cluster (UCC) ansatz, which is frequently employed in quantum chemistry, was investigated by O'Malley et al. (2016). They demonstrated that as the system size and molecular interaction complexity increase, so does the number of qubits needed for VQE implementations. Furthermore, Hempel et al. (2018) suggested techniques for calculating the quantum resources for VQE, especially when considering noisy NISQ devices. To lessen the effect of noise on estimates of quantum resources, they underlined the necessity of effective error mitigation strategies.

3. Quantum Error Correction and Physical Qubits.

Since quantum computers are prone to errors, quantum error correction is essential to scaling simulations of quantum chemistry to larger molecular systems. Error correction systems like surface codes and concatenated codes incur overhead that must be taken into account when estimating quantum resources. Fundamental work on the design of quantum error correction codes was done by Fowler et al. (2012) and Dennis et al. (2002), and it has since been expanded for use in quantum chemical applications.

The effect of error correction on quantum chemistry simulations was investigated by Bauer et al. (2016), who demonstrated that error correction can dramatically raise the number of physical qubits needed for a certain logical qubit. They pointed out that in order to provide dependable quantum computation for big molecule systems, error

correction is crucial. The significance of quantum error correction in upcoming quantum devices was further emphasized by Preskill (2018), particularly as fault-tolerant quantum computing draws near.

4. Estimation Tools and Software for Quantum Resource Calculation

For quantum chemistry simulations, a number of software tools and frameworks have been created to estimate the quantum resources. Features for quantum chemistry simulations, such as resource estimation for algorithms like QPE and VQE, are included in IBM's Qiskit quantum computing framework. In order to gain insight into gate counts and qubit utilization, Kandala et al. (2017) showed how to use Qiskit to simulate quantum chemistry problems on actual quantum gear.

The Quantum Resource Estimator (QRE), a tool created to forecast the quantum resources needed for simulating molecule characteristics using quantum chemistry algorithms, was presented by Motta et al. (2020). In order to help researchers determine if quantum chemistry simulations on near-term quantum devices are feasible, QRE determines the number of gates, qubits, and computational time needed for certain quantum chemistry problems. This paper emphasizes how crucial it is to have precise methods for resource assessment as quantum hardware advances.

5. Challenges and Future Directions

Accurately forecasting the quantum resources needed for real-world quantum chemistry applications is still difficult despite advancements in quantum resource prediction. The scalability of quantum algorithms is one of the main issues since the necessary quantum resources increase quickly with system size and accuracy. To lower resource requirements and increase the viability of quantum chemistry simulations on near-term quantum computers, researchers are refining quantum algorithms and error correction techniques.

The extension of quantum resource estimating tools to accommodate a broader variety of quantum chemistry techniques, including density functional theory (DFT), Hartree-Fock theory, and the Coupled Cluster (CC) method, is another area of future research. Researchers can more accurately evaluate the entire potential of quantum computing for resolving challenging chemical issues by incorporating these techniques into quantum resource estimators.

Methodologies

Figure 1 shows the Quantum Resource Estimator (QRE) program's design as suggested in this study. Three separate input blocks (upper, lower, and left blocks) and one output block (right block) make up the QRE program. Together, these elements offer a thorough assessment of the quantum resources needed for applications in quantum chemistry. Capturing the chemical characteristics of the molecular system under study is the primary function of the first input block, which is situated at the top (upper block). This block contains important details about the molecules, including the sorts of atoms, electrical charges, the level of theory used in the calculations, the basis sets selected, and the required chemical accuracy. The resource estimation procedure is based on these factors, which specify the particular molecular system in question. The computational aspects of the quantum hardware and algorithms are the emphasis of the second input block, which is located on the left (left block). Important parameters like qubit connectivity—which establishes how qubits can communicate with one another on a particular quantum processor—gate fidelities and gate times—which indicate the precision and duration of quantum gate operations—measurement errors—which count possible errors in qubit measurement—and sampling rates—which specify the frequency of measurements made while the algorithm is running—are all included.

When combined, these inputs give the QRE algorithm the full set of data it needs to calculate the quantum resources required to accurately simulate the molecular system. The output block (right block) then determines the quantum resources required to execute the quantum chemistry algorithms on the specified quantum computer hardware, including the number of qubits, gate operations, and runtime.

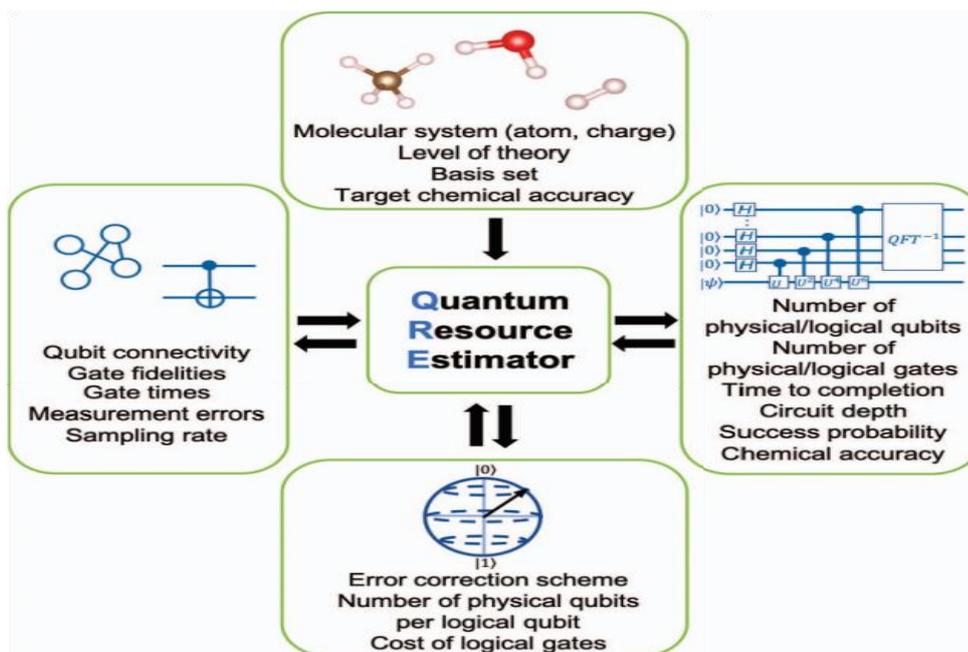


Fig. 1. Schematic diagram of QRE.

The error correction technique, which is the last input block at the bottom (lower block), is essential for calculating how many physical qubits are needed for each logical qubit. Error correction is required to enable dependable computation because quantum computers are intrinsically prone to errors. Taking into consideration the overhead imposed by error correction protocols, this block enables the QRE software to determine the number of physical qubits required to implement logical qubits.

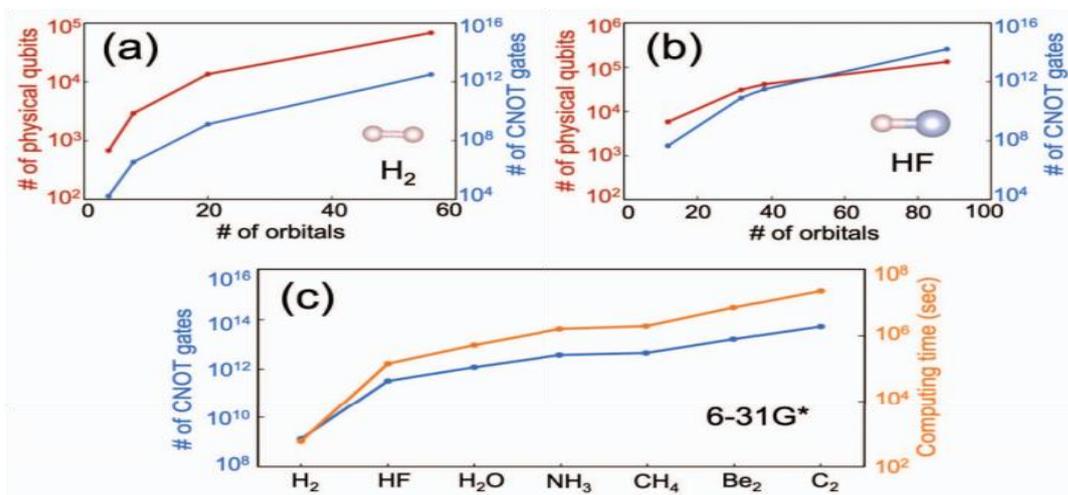
The upper, left, and right blocks have been the main focus of the QRE program's development thus far because they are crucial for producing the resource estimates needed for applications in quantum chemistry. Three essential steps comprise the resource estimation process in QRE:

1. **Creation of Electronic Integral Files:** For every molecule, electronic integral files must first be created. The molecular details—such as atom types, molecular geometries, charges, and the selected basis sets—provided in the upper input block are used to generate these files. The PySCF package, a popular Python-based computational chemistry framework that manages quantum chemical computations, including integrals needed for molecular system simulation, is used to generate the integral files [1], [2].
2. **Trotter Step Gate Count** In the quantum phase estimation (QPE) technique, the next step is to determine how many quantum gates are needed for a single Trotter step. The gate count code included in the Microsoft Quantum Development Kit (QDK) is used to do this [3]. The gate count code determines how many rotation gates and CNOT gates are required for a single Trotter step, a crucial part of the QPE algorithm, using the previously created electronic integral files as input.
3. **Estimation of Quantum Resources:** Lastly, the QRE software calculates the total quantum resources needed to run the entire QPE method. This comprises the required physical qubits, the anticipated calculation time, and the total number of gates. These estimations take into account the algorithmic mistakes (such as flaws in the quantum phase estimation procedure and other computational stages) as well as the physical characteristics of the quantum device (such as qubit connectivity and gate fidelities) [4]–[6]. As a result, the resources required to correctly execute the quantum chemistry algorithm on an actual quantum computer can be predicted with greater accuracy.

The QRE program facilitates the practical use of quantum computing to quantum chemistry simulations by offering a thorough resource estimation through these three processes.

RESULT AND DISCUSSION

Using a variety of basis sets, including STO-3G, STO-6G, 6-31G*, and cc-pVDZ, we conducted a thorough estimation of the quantum resources needed for quantum phase estimation (QPE) in order to calculate the chemical properties of several molecules, including H₂, HF, H₂O, NH₃, CH₄, Be₂, and C₂. To enable a comprehensive examination, these molecules were chosen to represent a range of chemical systems, and resource estimation was performed across these various sets of computational settings.



The key quantum resource metrics estimated include:

- The quantity of rotation and CNOT gates needed for the QPE algorithm.
- The number of sequential quantum gate operations required is indicated by the circuit depth.
- The amount of time needed to finish the QPE calculation.
- the quantity of physical qubits required by the quantum computer for logical qubit representation and error correction.

The trend seen in our resource estimation is graphically depicted in Figure 2, which shows that the number of physical qubits, CNOT gates, and overall computation time required all rise in tandem with the number of orbitals in the molecular system. This pattern emphasizes how difficult it is to simulate bigger molecules with more intricate orbital interactions and electron configurations, which inevitably necessitates more computational power for both gate operations and actual qubit utilization.

The difficulties in scaling quantum chemistry simulations to larger, more complicated molecules using quantum computers are shown by this increase in resource requirements as a function of molecular size and orbital count. Understanding the viability of using quantum computing in actual chemical systems requires such knowledge.

CONCLUSION

In order to effectively and methodically quantify the quantum resources needed to use quantum computers to solve quantum chemistry issues, we created the Quantum Resource Estimator (QRE) software. This tool offers a thorough evaluation of the computational resources required to model molecular systems and calculate their chemical properties, including gate counts, circuit depth, and physical qubits. QRE provides a thorough assessment of the necessary quantum resources, which helps determine whether using quantum computing to solve practical quantum chemistry problems is feasible.

We are continually working to add new features to QRE in addition to its current capabilities. The error correction system, which will improve the program's capacity to predict the quantity of physical qubits required for error-tolerant quantum computing, is one important area of development. Additionally, in order to enable QRE to estimate resources for a wider variety of quantum chemistry issues, we are incorporating the Unitary Coupled Cluster (UCC) ansatz for the Variational Quantum Eigensolver (VQE) method. The UCC ansatz is a potent technique for characterizing electronic wavefunctions and is especially crucial for accurately researching bigger molecule systems.

With these improvements, QRE will become even more flexible, assisting engineers and researchers in determining the quantum resource requirements of a broad range of quantum chemistry algorithms. Future quantum device design and optimization are anticipated to be significantly influenced by the ongoing development of QRE and related software tools. These tools will also open the door for the actual implementation of quantum chemistry on quantum computers by offering insightful information about the potential of quantum computing to resolve challenging chemical challenges. The resource estimates for compounds such as HF and H₂_22 are shown in Figure 2. Panel (b) displays comparable statistics for HF, but Panel (a) displays the number of physical qubits and CNOT gates for H₂_22. Panel (c) illustrates how molecular complexity affects the need for quantum resources by comparing the CNOT gate counts and total computation time for different molecules using the 6-31G* basis set.

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