

Lost pixel restoration using pentagonal fuzzy numbers

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ABSTRACT

The modern technological development has created a scenario in the handling of images, with the digital images becoming almost monopoly. While digital images enjoy a high degree of usage benefits, there are certain challenges faced by the users of these images owing to the inherent problems in capturing and storing them. One such problem that manifests in digital images is the problem of lost pixels. There are many methods used in the literature to address these problems and many used to retrieve or replace the lost pixels in practice. In this paper, we introduce a new method to replace a lost pixels based on pentagonal fuzzy numbers.

Keywords: Pentagonal fuzzy numbers, lost pixels

INTRODUCTION

Digital image processing is an area of research that has attracted the attention of researchers in computer science and mathematics owing to the immediate application value in this area. Researchers have considered many aspects of digital image processing. It is often seen that the digital images suffer quality when the pixels [1] are either lost or undergoes unexpected changes. It has been often realized that some pixels are lost while using a digital image in some stage of its usage, which is very common in satellite images. When pixels are lost, it diminishes the quality of the images, sometimes to undesired proportions. Hence it becomes inevitable that the pixel value of the lost pixels is somehow made up for either by recreation of the original image when it is possible and often by replacing by a good approximation. Many algorithms have been designed by researchers for replacing the lost pixels to a desired level of accuracy [9, 8, 7]. The success of these algorithms lies in not only approximating the lost pixel value to an acceptable nearness to the lost pixel value, but also in the ease with which the algorithm can be employed for computing such values and the effortlessness with which the algorithm can approximate such pixel values. Most of the algorithms used for retrieving the lost pixel value relies on the fact that any pixel will on an average behave only as its neighbouring pixels. So, it is customary that all these algorithms use the pixel value of the pixels in the neighbourhood of the lost pixel.

A digital image is logically organized as rows and columns of elements called pixels that make up the whole image. A pixel is the smallest unit of an image and has several attributes such as the colour, brightness and the background. A pixel is characterized by a number called the pixel value, which is typically an integer in the range 0 to 255. When a pixel is lost, it is to be understood that the integer value associated with that pixel is lost. Hence one has to make up for the lost pixel value by providing either the exact value or an alternate value to the lost pixel value without much of an error. Otherwise, the quality suffered by the image on account of a lost pixel may even be more complicated if an inappropriate value is used to replace it. Hence the problem of lost pixels has to be handled with at most care so that the experience or information that an image will provide will be completely lost.

Fuzzy numbers have dominated several domains of research due to their versatility and immediate solutions they provide. Many fuzzy numbers have been used by the researchers such as the triangular fuzzy numbers [2], trapezoidal fuzzy numbers [4], pentagonal fuzzy numbers [6], octagonal fuzzy numbers [5] and so on. For pixel restoration, fuzzy numbers can be used in combination with a ranking method. In this paper, we use the generalized pentagonal fuzzy numbers to restore a lost pixel value of an image.

We consider the pentagonal fuzzy numbers and consider a number of pentagonal fuzzy numbers to represent the lost pixel value and for the ranking function of the pentagonal fuzzy numbers, we use the ranking function proposed in [3]. For defuzzification, we use the proposed ranking function, by taking the floor in order that the rank represents a pixel value.

PIXEL RESTORATION METHOD

We assume that the lost pixel is X and is at the centre of the following table, which is part of the pixelate of the image. For the restoration process, we consider the pentagonal fuzzy numbers, $\tilde{A} = (g, h, i, l, m)$, $\tilde{B} = (g, l, p, h, q)$, $\tilde{C} = (i, m, r, h, q)$ and $\tilde{D} = (p, q, r, l, m)$. We then rank these fuzzy numbers as prescribed in [3]. We then find the fuzzy number with minimum amongst the ranks and choose it to represent the lost pixel value. The number is assumed to have been defuzzified by the ranking functions considered by taking the floor value of the rank, where necessary to arrive at a value between 0 and 255.

| | | | | |
|-----|-----|-----|-----|-----|
| a | b | c | D | e |
| f | g | h | I | j |
| k | l | X | M | n |
| O | p | q | R | s |
| t | u | v | W | y |

We illustrate the above method with the aid of an example. Consider the following pixel matrix of part of an image which contains a lost pixel. We shall retrieve the lost pixel value using the method suggested.

| | | | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 122 | 130 | 138 | 139 | 134 | 136 | 126 | 144 | 150 | 156 |
| 125 | 132 | 138 | 145 | 140 | 140 | 130 | 140 | 152 | 162 |
| 127 | 133 | 142 | 145 | 146 | 141 | 134 | 147 | 154 | 158 |
| 135 | 134 | 147 | 149 | X | 142 | 140 | 143 | 149 | 153 |
| 137 | 140 | 151 | 152 | 148 | 152 | 143 | 147 | 154 | 156 |
| 142 | 144 | 149 | 160 | 154 | 159 | 148 | 154 | 162 | 168 |
| 146 | 145 | 147 | 155 | 158 | 162 | 156 | 158 | 169 | 171 |
| 150 | 149 | 155 | 162 | 165 | 167 | 161 | 167 | 179 | 182 |
| 152 | 158 | 164 | 173 | 177 | 179 | 182 | 188 | 196 | 208 |
| 155 | 160 | 171 | 177 | 183 | 180 | 185 | 193 | 201 | 211 |

Table 1

We first form the four pentagonal fuzzy numbers $\tilde{A} = (g, h, i, l, m)$, $\tilde{B} = (g, l, p, h, q)$, $\tilde{C} = (i, m, r, h, q)$ and $\tilde{D} = (p, q, r, l, m)$ from the following submatrix of the above matrix.

| | | |
|-----|-----|-----|
| 145 | 146 | 141 |
| 149 | X | 142 |
| 152 | 148 | 152 |

The pentagonal fuzzy numbers considered from Table 1 are, $\tilde{A} = (145, 146, 141, 149, 142)$, $\tilde{B} = (145, 149, 152, 146, 148)$, $\tilde{C} = (141, 142, 152, 146, 148)$ and $\tilde{D} = (152, 148, 152, 149, 142)$. Following the ranking method suggested, we obtain, $R(\tilde{A}) = 144$, $R(\tilde{B}) = 149$, $R(\tilde{C}) = 147$ and $R(\tilde{D}) = 149$. The maximum of these ranks is 149.1929, corresponding to the fuzzy number \tilde{D} . Defuzzifying, we get the value of X as 149, taking the floor.

CONCLUSION

The above method is a simple method and more pentagonal fuzzy numbers can be considered than the ones used in the suggested method. Using a greater number of fuzzy sets will improve the reliability of the fuzzification-defuzzification process. We see that retrieved value of X in the illustration is more like the values in the neighbourhood of the lost pixel value X .

REFERENCES

- [1]. James F. Blinn, IEEE engineering in medicine and biology magazine: the quarterly magazine of Engineering in Medicine & Biology Society, 25(5) (2005), 82 – 87
- [2]. Emrah Akyar, Handan Akyar and Serkan Ali Duzce, A New Method for Ranking Triangular Fuzzy Numbers, International Journal of Uncertainty, Fuzziness and Knowledge-Based Systems, 20(5) (2012), 729 – 740
- [3]. Fahrudin Muhtarullo and AtiaNuraini, Performance Evaluation of New Ranking Function Methods with Current Ranking Functions Using VAM and MM-VAM, Advances in Social Science, Education, and Humanities Research, Volume 550 (2021), 418 – 424
- [4]. K. Ganesan and P. Veeramani, Fuzzy linear programs with trapezoidal fuzzy numbers, Annals of Operations Research, Vol. 143 (2006), 305 – 315
- [5]. S.U. Malini and Felbin C. Kennedy, An Approach for Solving Fuzzy Transportation Problem Using Octagonal Fuzzy Numbers, Applied Mathematical Sciences, Vol. 7(54) (2013), 2661 – 2673
- [6]. S. Rajeswari et al., Optimization in Fuzzy Economic Order Quantity Model Involving Pentagonal Fuzzy Numbers, International Journal of Fuzzy Systems, 24 (2022), 44 – 56
- [7]. Shilpa Rani, Sonika Jindal and Bhavneet Kaur, A Brief Review on Image Restoration Techniques, International Journal of Computer Application, 150(12) (2016), 30 – 33
- [8]. Teruo Akiyama et al., "Faxed document image restoration method based on local pixel patterns," Proc. SPIE 3305, Document Recognition V, (1 April 1998), <https://doi.org/10.1117/12.304637>
- [9]. Zhang Leihong et al., Restoration of Single pixel imaging in atmospheric turbulence by Fourier filter and CGAN, Applied Physics B, 127, 45 (2021), <https://doi.org/10.1007/s00340-021-07596-8>