Optical Constants of KDPTGS Single Crystals

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Abstract: Single crystals of KDP doped TGS crystals (KDPTGS) were synthesized and grown by slow evaporation solution growth technique. KDPTGS easily crystallizes in monoclinic system with space group P2_1/c. Using the transmittance and reflectance spectra, the optical energy gap and optical constants have been determined. Peculiar changes in the optical constants of single crystals of triglycine sulfate (TGS) pure and doped with different concentrations of potassium dihydrogen phosphate. It was found that, the absorption coefficient (α), indirect optical band gap (E_g^ind), refractive index (n) and the extinction coefficient (k) decreased with increasing dopant concentration. The refractive index dispersion data were analyzed using the Wemple-Di Domenico single-effective-oscillator model. As a result, the oscillator energy, dispersion energy, oscillator strength, and zero-frequency refractive index were determined. The values obtained for the single-oscillator energy E_ω are nearly consistent with the optical gap results. The dependence of the optical constants of KDPTGS on the photon energy (ℏω) at different concentrations of KDP were discussed.

Keywords: KDPTGS crystals, Optical energy gap, Normal dispersion, Optical constants.

1- Introduction

Crystals of triglycine sulfate abbreviated as (TGS) is a well-known ferroelectric material, find wide application as room temperature IR detectors [1, 2]. TGS is one of the very few ferroelectrics known to exhibit a second-order phase transition and hence offers possibilities for the observation of genuine critical phenomenon very close to the Curie temperature. TGS is an order-disorder type ferroelectrics with a transition from ferroelectric to paraelectric phase at 322 K, having high pyroelectric coefficient and low dielectric constant values [3].

Ferroelectric properties of TGS crystals have been found to change strongly under the action of different kinds of admixtures [4,5]. Many authors have investigated the effect of various doping on TGS [6-11]. Single crystals of triglycine sulfate (TGS) doped with various L-form amino acids (L-valine, L-leucine, and L-isoleucine) have been prepared by Nakatani et al. [12]. Doping effects on the crystal morphology and the ferroelectric domain structure, and the generation of internal bias field were investigated. For crystals grown from solutions with L-valine, L-leucine, and L-isoleucine, both the morphology and the domain structures were resemble to pure TGS. Many studies have been performed with different metallic ion dopants such as Cu^{2+}, Li^{+}, Mn^{2+}, Ni^{2+}, Cr^{3+}, which have been added to modify the properties of TGS crystals[13-16]. Rare earth metal ions admixture TGS crystals, such as La, Ce and Nd modified the morphology and coercive field values[13].

The interest in studying pure and doped TGS crystals has increased because of their promise in various devices. Several dopants have been recently used, more or less successful, to inhibit the ferroelectric switching of TGS, in order to increase crystal unipolarity and the figure of merit of material[14]. The influence of the KDP doping on the pyroelectric and the dielectric properties of the TGS crystal was studied by Sooman Leet al. [17]. Their results confirmed that, with increasing KDP doping, the coercive field increased and the Curie temperature decreased. Moreover, improved pyroelectric properties were observed.

The optical constants define how light interacts with a material. The determination of these optical constants is expected to expand the available physical information about the spectral dependence of optical parameters such as refractive index, dielectric constant, reflectivity and absorption coefficients are essential in characterizing materials that are used in the fabrication of optoelectronic devices[18].

The investigations on TGS doped with ferroelectric and antiferroelectric crystals are not studied in details. In the present work, the influence of KDP dopant concentration on the TGS crystal optical parameters has been studied. The dispersion of the refractive index is discussed in terms of the Wemple-DiDomenico single-effective-oscillator model. The refractive
index dispersion parameters: oscillator energy, dispersion energy, oscillator strength, and zero-frequency refractive index were estimated.

2-Experimental Procedures

Single crystals of TGS (NH₂CH₂COOH)₂H₂SO₄ doped with different concentrations of potassium dihydrogen phosphate KH₂PO₄ (KDP) were grown by the slow evaporation method in the ferroelectric phase at about 315 K. The concentrations of KDP were 10%, 20%, 30%, 40% and 50% relative to H₂SO₄. The calculated amount of material was dissolved in double distilled water at room temperature and the reactants were thoroughly dissolved and stirred well for about 6 hours using a temperature controlled magnetic stirrer to obtain a homogeneous mixture of solution. The solution was allowed to evaporate at room temperature, which yielded colorless crystalline salt of KDPTGS. The purity of the synthesized compound was further improved by successive recrystallization process. The saturated solution (about 400 ml) was prepared at room temperature based on solubility data by using water as a solvent. To eliminate difference in growth condition from our discussions, crystals with different KDP concentrations were grown simultaneously in a multi-jar crystallizer.

After preliminary experiments, optimum growth parameters including solution purity, seed, orientation and purity, seed rotational speed, starting temperature of crystallization and period of growing crystal were chosen for best result. After 2–3 weeks a single nucleation started and seed crystals with were harvested. Good optical quality seed crystals free from defects and inclusions are used for the growth of crystals from its saturated solution using suspended seed technique. After a span of about 30 days flawlessness crystals of optical quality and with well-developed faces were obtained sizes upto 25×15×4 mm³. The normal external shape (habit) of doped crystals is modified due to unequal growth rate along the ferroelectric axis in opposite directions. The crystals are transparent and their shape and size is sensitive to the amount of KDP in the solution during growth. With increasing concentration of KDP in solution, the size of the crystals increases up to a molar concentration of 20–30% of KDP and decreases at a higher concentration. More details about the grown crystals are shown elsewhere [19]. The amount of KDP (mol%) incorporated into the crystal is very low. It was reported that, a factor of 10⁻² in comparison to the actual amount taken in the solution obtained for the amount of H₂PO₄ present in the solution of TGSP crystals [20].

The crystals were cleaved parallel to (010) plane and then reduced to the required thickness. In most cases, this thickness was in the order of 1 mm. Cleaved rectangular b-cut plates about 20 mm² in area and 1 mm in thickness specimens were prepared and then polished on a wet piece of soft cloth to be used for optical measurements. The samples used for measurements were clear, transparent and free from any noticeable defects. Specimens prepared with these dimensions to fit the sample holder, and the sample was fixed to the holder by special glue. The optical transmission spectra measured in the photon energy range 190-900 nm at room temperature were determined using Shimadzu UV-VIS-2101 PC dual beam scanning spectrophotometer. The incident unpolarized light was nearly perpendicular to b-plane. The surrounding medium was air. For the same samples, the optical reflectance was recorded by using the same spectrophotometer in the same wavelength range. The reflectance measurements were made using specular reflectance attachment at an incidence angle of 5°, where the sample should be placed horizontally on the stage facing downward and was illuminated from the bottom. Reflectance measurements were performed, also, at room temperature.

3-Results and discussion

3.1. Optical transition

The transmittance T(λ) and reflectance R(λ) spectra are shown in Fig. 1. By using those spectrums, the optical energy gap and optical constants have been determined. Fig. 1-a shows the spectral distribution of transmittance in the spectral range 200–800 nm. The transmittance spectra of TGSK crystals decrease with increasing KDP ratio. Transmittance (T) gradually rises towards longer wavelength until it reaches its maximum value at about 350 nm. At shorter wavelengths, transmittance decreases rather quickly, and approaches near zero at around 230 nm. It is obvious that transmission edge is slightly affected by the KDP doping. It is also observed that the intensity of transmittance within the absorption region decreases by increasing KDP ratio. The reflectance spectra (Fig. 1-b) of the crystals show some peaks lies in the wavelength range of 200-500 nm, then show a slight decrease with the increase in wavelength up to 800 nm.

The absorption spectra of KDPTGS single crystals have been investigated at photon energies near the fundamental absorption region, and the absorption coefficient (α) obeys the equation [21]:

\[ \alpha(\omega) \propto (\omega_0 - \omega)^n \]  

where \( \omega_0 \) is the energy gap, \( n \) is the order of transition, and \( \omega \) is the frequency of the incident light.
where,  is the energy of incident photon,  is the optical energy gap and  is an exponent which can be assumed to have values of 1/2, 3/2, 2 and 3, depending on the nature of electronic transition responsible for absorption. Parameter  for allowed direct transition,  represents forbidden direct transition,  for allowed indirect transition and  for forbidden indirect transition. To determine the type of optical transition, we have examined  and found that the last relation yielded a linear dependence, which describes allowed indirect transitions. The energy gap is determined by plotting  as a function of  as depicted in Fig. 2 and taking the extrapolation of the linear portion of the curve to  = 0. The indirect energy gap value was found to be as shown in the inset of Fig. 2, and listed in Table 1. The presented data reveals that the increase of KDP concentration leads to an increase of the band gap  and saturates at 30 mol% of KDP doping, which is nearly similar with data presented in literature [22]. Their single crystal and powder XRD studies confirmed that a certain amount of HNO₃ is doped into TGS and that there is saturation in the doping level already at 20 mol% HNO₃ addition. Further increase in HNO₃ content in solution acted as additive and enabled the changes only in crystal habit.

### 3.2. Normal dispersion and its parameters

#### 3.2.1. Refractive index and extinction coefficient

The complex refractive index is a representation of the optical constants of material and is represented by . The real part ‘n’ is the index of refraction, defines the phase velocity of light in material:  where  is the speed of light in material and  is the speed of light in vacuum. The imaginary part ‘k’ is the extinction coefficient, determines how fast the amplitude of the wave decreases. The extinction coefficient is directly related to the absorption of material and is related to the absorption coefficient by:  where,  is the absorption coefficient and  is the wavelength of light. The reflectance (R) in terms of the absorption coefficient and refractive index (n) can be derived from the relations [23]:

\[
n = \frac{1 + \sqrt{\epsilon}}{1 - \sqrt{\epsilon}}
\]

The extinction coefficient (k) can be calculated using the equation:

\[
k = \frac{\alpha \lambda}{4\pi}
\]

The frequency dispersion of characterizes completely the propagation, reflection and loss of light in material. This provides us with information about the electronic structure of the material. Therefore,  is an important quantity for the design of highly efficient optoelectronic devices [24]. The complex dielectric constant is described by:

\[
\tilde{\epsilon} = \epsilon_r - i\epsilon_i \quad \text{And} \quad \tan \delta = \frac{\epsilon_i}{\epsilon_r}
\]

The real  and imaginary  parts of the dielectric constant are related to n and k by the relations:

\[
\epsilon_r = n^2 - k^2
\]

\[
\epsilon_i = 2nk
\]

The variation of refraction index (n), extinction coefficient (k), real (εᵣ) and imaginary (εᵢ) parts of the dielectric constant as a function of wavelength λ for TGS crystal doped with different concentrations of KDP ratio is shown in Figs. 3 & 4. Fig. 3-a shows the obtained spectral variation of the refractive index n in the wavelength range 200–800 nm, for TGS crystals doped with different KDP ratios. KDPTGS crystals showed similar behavior of n vs. λ and the values differ with KDP ratio. It also shows anomalous dispersion at wavelengths λ < 450 nm exhibiting various peaks. At wavelengths λ > 450 nm, in the non-absorbing region, the variation shows normal dispersion. An absorption band is observed in the wavelength range 250-280 nm and other two absorption bands in the wavelength ranges 330–360 and 400–500 nm. The amplitude of these bands decreases upon increasing KDP ratio. Further, the refractive index decreases with increasing the KDP ratio; this may be due to doping TGS with KDP which could change the density and/or the polarization of the grown crystal. From Fig. 3-b, we can see that the extinction coefficient k reverse the behavior of the transmittance. It is clear from Fig. 4 that the variation of  follows the same trend as that of n, whereas the variation of  mainly follows the behavior of k which is related to the variation of  with photon energy. The real dielectric constant shows values larger than that for imaginary dielectric constant at the studied photon energy. The variation of the dielectric constant with photon energy indicates that different
interactions between photons and electrons in KDPTGS crystals are reproduced in this energy range. These interactions are observed on the shapes and cause formation of peaks in the dielectric spectra which depends on the material type. The real and imaginary parts of the dielectric constant \( \varepsilon_r \) and \( \varepsilon_i \) can be also used to calculate the spectral behavior of the optical conductivity according to the following relations [25]:

\[
\sigma^* = \sigma_r + i\sigma_i \quad (7)
\]

\[
\sigma_r = \omega \varepsilon_o \varepsilon_2 \text{ and } \sigma_i = \omega \varepsilon_o \varepsilon_1 \quad (8)
\]

Where \( \omega \) is the angular frequency, \( \varepsilon_o \) is the permittivity of free space. The spectra of real and imaginary parts of the optical conductivity are shown in Fig.5. It can be seen that both the real and imaginary part increases with increasing the photon energy up to 2.6 eV which can be attributed to excitation of electrons by photon energy. Real part of optical conductivity continues increasing sharply beyond 5.2 eV of photon energy as seen in Fig. 5 suggesting strong excitation of the electrons. The optical conductivities \( \sigma_r \) and \( \sigma_i \) can be used to detect any further interband transitions. From the obtained data in Fig.5, it is noted that there are one distinct peaks for both \( \sigma_r \) and \( \sigma_i \) for different KDP ratios. The origin of this one peak in each ratio may be attributed to the optical interband transition. The increased of optical conductivity at high photon energies is due to the high absorbance of KDPTGS crystals and may be due to electron excited by photon energy.

For further analysis of the experimental results, the electric susceptibility \( \chi_e \) can be calculated according to the relation [26]:

\[
\chi_e = \varepsilon_r - 4\pi \varepsilon_0 = n^2 - k^2 \quad (9)
\]

\[
\chi_e = \frac{(\omega^2-k^2-\varepsilon_0)}{4\pi} \quad (10)
\]

Where, \( \varepsilon_o \) is the dielectric constant in the absence of any contribution from free carriers. The values of electric susceptibility \( \chi_e \) for KDPTGS crystals were plotted in Fig. 6 and the calculated values at 5 eV are listed in Table 1.

### 3.2.2. Wemple–DiDemenico dispersion relation

The data of the spectral dependence of the refractive index in the transparent region, at low optical frequencies could be analyzed in terms of a single oscillator model, following the parameterization suggested by Wemple and DiDemenico [27, 28]. The dispersive refractive index data in \( \omega < \omega_{opt} \) range were analyzed according to the single-effective-oscillator model proposed by Wemple and DiDemenico. The refractive index is related to photon energy through the relationship:

\[
n^2 = 1 + \frac{E_{so}^2}{E_{so}^2 - (\hbar \omega)^2} \quad (11)
\]

Where, \( E_{so} \) is the single oscillator energy and \( E_d \) is the dispersion energy. Values of the parameters \( (E_{so} \) and \( E_d) \) can be evaluated by plotting of \( (n^2-1)^{-1} \) versus \( (\hbar \omega)^2 \) and fitting it to a straight line as shown in Fig.7. From the fitting the found values are given in Table 1.

The moments of optical dispersion spectra \( M_{-1} \) and \( M_{-3} \) can be evaluated using the relationships [25]:

\[
E_{so}^2 = \frac{M_{-1}}{M_{-3}} \quad (12)
\]

\[
E_d^2 = \frac{M_{-1}^2}{M_{-3}} \quad (13)
\]

The zero-frequency refractive index (static refractive index) is obtained using eq. (11), by putting \( \hbar \omega = 0 \), i.e. based on the expression:

\[
n_0^2 - 1 = \frac{E_d}{E_{so}} \quad (14)
\]

Furthermore the values of static refractive index (zero-frequency refractive index) \( n_0 \) are also calculated and recorded in Table 1. In terms of \( n_0 \), one can see its decreasing with increasing KDP concentration which means that the static dielectric constant \( \varepsilon_{sta} \) (dielectric constant at \( \hbar \omega = 0 \)) will be smaller after doping TGS crystal with KDP. This can be explained by rewriting eq. (14) as \( \varepsilon_{sta} = n_0^2 \). The values are shown in Tables 1, 2.
The values of dispersion parameters and the optical moments of KDP doped TGS gathered in Table. 1 are strongly agree with Wemple [27] and Di Domentic [28]. It is clear from the table that both values of single oscillator energy (E_s) and dispersion energy (E_d) decrease. Decreasing the single oscillator energy E_s (decreasing the oscillator natural frequency \( \omega_0 \)) with increasing KDP concentration means that the normal dispersion region of TGS crystal shifts to a range of lower photon energies by doping it with KDP. On the other hand, decreasing the dispersion energy E_d with increasing KDP concentration means that the intensity of the interband optical transitions of TGS crystal decreases by doping it with KDP. In addition, doping TGS crystal with KDP leads to decreasing its dispersion \( \frac{dn}{dE} \) due to the increase of the slope \( \frac{d(n^2-1)}{d(\omega^2)} \) with increasing KDP concentration as it is clear in Fig. 7.

### Table 1. Normal dispersion of pure TGS and KDP doped TGS single crystals.

<table>
<thead>
<tr>
<th>KDP ratio (mol%)</th>
<th>( E_{g}^{\text{opt}} ) (eV)</th>
<th>( E_s ) (eV)</th>
<th>( E_d ) (eV)</th>
<th>( M_{-1} ) (eV)^2</th>
<th>( M_{-3} ) (eV)^2</th>
<th>( \chi_e )</th>
<th>( n_0 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 (pure)</td>
<td>4.912</td>
<td>5.006</td>
<td>6.604</td>
<td>1.319</td>
<td>0.053</td>
<td>0.315</td>
<td>1.523</td>
</tr>
<tr>
<td>10</td>
<td>4.915</td>
<td>4.946</td>
<td>5.683</td>
<td>1.149</td>
<td>0.047</td>
<td>0.258</td>
<td>1.466</td>
</tr>
<tr>
<td>20</td>
<td>4.928</td>
<td>6.337</td>
<td>8.08</td>
<td>1.275</td>
<td>0.032</td>
<td>0.212</td>
<td>1.508</td>
</tr>
<tr>
<td>30</td>
<td>4.963</td>
<td>6.061</td>
<td>5.922</td>
<td>0.977</td>
<td>0.027</td>
<td>0.202</td>
<td>1.406</td>
</tr>
<tr>
<td>40</td>
<td>4.966</td>
<td>5.157</td>
<td>3.919</td>
<td>0.76</td>
<td>0.029</td>
<td>0.185</td>
<td>1.327</td>
</tr>
<tr>
<td>50</td>
<td>4.969</td>
<td>4.121</td>
<td>1.965</td>
<td>0.477</td>
<td>0.028</td>
<td>0.173</td>
<td>1.215</td>
</tr>
</tbody>
</table>

The refractive index n can also be analyzed to determine the oscillator strength \( S_{so} \) for KDPTGS crystals. The refractive index is represented by a single Sellmeier oscillator at low energies [29]:

\[
\frac{n^2-1}{n^2-1} = 1 - \left( \frac{\lambda_{so}}{\lambda_0} \right)^2
\]  

(15)

Where \( \lambda_{so} \) is the oscillator wavelength. If we put \( S_{so} = (n_0^2 - 1)/\lambda_{so}^2 \). We can rewrite Eq. (15) as:

\[
\frac{1}{n^2-1} = \frac{1}{\lambda_{so}^2 S_{so}} - \frac{1}{\lambda_{so}^2 S_{so}}
\]

(16)

\( S_{so} \) is the average oscillator strength. The plotting of \( (n^2-1)^{-1} \) versus \( \lambda^{-2} \) shows linear part edge as shown in Fig. 8. The intersection with \( (n^2-1)^{-1} \) axis is \( 1/\lambda_{so}^2 S_{so} \) and the slope is \( 1/S_{so} \). Hence, the values of \( S_{so} \), \( \lambda_{so} \), and \( n_0 \) were determined and listed in Table. 2.

#### 3.2.3 Lattice dielectric constant \( \varepsilon_L \) and contribution of charge carrier (N)

The obtained data of refractive index n, can be analyzed to obtain the lattice dielectric constant \( \varepsilon_L \). The relation between optical real part of dielectric constant \( \varepsilon_r \) and the square of wavelength \( \lambda^2 \) is given by [30]:

\[
\varepsilon_r = \frac{n^2 - k^2}{n^2 - 1} = \varepsilon_L - \frac{e^2}{4m^2c^2\varepsilon_0 \lambda^2} \frac{N}{m^*}
\]

(17)

Where \( e \) is the electronic charge, \( \varepsilon_L \) is infinite high frequency dielectric constant, \( \varepsilon_0 \) the permittivity of free space \( (8.854 \times 10^{-12} \ F/\mu m^2) \). c is the velocity of light, and \( N/m^* \) is the ratio of carrier concentration to the effective mass. The lattice dielectric constant \( \varepsilon_L \) can be obtained from plotting \( n^2 \) as a function of \( \lambda^2 \) as shown in Fig. 9. Extrapolating the linear part of this dependence to zero wavelength give value of \( \varepsilon_L \) and from the slope the values of \( N/m^* \) were calculated. The obtained values of \( \varepsilon_L \) and \( N/m^* \) are given in the Table. 2. It can be noticed that the \( N/m^* \) ratio decreases with increasing KDP concentration. In general, \( N/m^* \) ratio is related to the internal microstructure. Most of the
changes in the N/m^2 ratio are corresponding to the change in the carrier concentration N. Such behavior may be interpreted as that increasing KDP ratio creates additional trapping carriers which unite with the original carrier in the grown crystal.

Table 2. Optical parameters of pure TGS and KDP doped TGS single crystals.

<table>
<thead>
<tr>
<th>KDP ratio (mol%)</th>
<th>N/m^2 (m^3 kg^{-1})</th>
<th>λ_{so} (nm)</th>
<th>S_{so}(nm)^{-2}</th>
<th>ε_L</th>
<th>ε_{sta.}</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 (pure)</td>
<td>2.959 x 10^{27}</td>
<td>261.083</td>
<td>1.871 x 10^{-5}</td>
<td>3.361</td>
<td>2.319</td>
</tr>
<tr>
<td>10</td>
<td>2.668 x 10^{27}</td>
<td>258.998</td>
<td>1.678 x 10^{-5}</td>
<td>3.087</td>
<td>2.149</td>
</tr>
<tr>
<td>20</td>
<td>1.408 x 10^{27}</td>
<td>202.164</td>
<td>3.085 x 10^{-5}</td>
<td>2.797</td>
<td>2.275</td>
</tr>
<tr>
<td>30</td>
<td>1.214 x 10^{27}</td>
<td>211.969</td>
<td>2.147 x 10^{-5}</td>
<td>2.425</td>
<td>1.977</td>
</tr>
<tr>
<td>40</td>
<td>1.476 x 10^{27}</td>
<td>240.757</td>
<td>1.312 x 10^{-5}</td>
<td>2.294</td>
<td>1.76</td>
</tr>
<tr>
<td>50</td>
<td>2.137 x 10^{27}</td>
<td>302.992</td>
<td>0.513 x 10^{-5}</td>
<td>2.191</td>
<td>1.477</td>
</tr>
</tbody>
</table>

Conclusions

From the absorbance and reflectance spectra for KDPTGS crystals, we observed that the absorption bands shift towards the smaller wavelength with the increase of KDP concentration, and the value of transmission and reflection decreases with the increases of KDP ratio. The indirect optical energy gap for the grown crystals decreases with the increase of dopant concentration. Optical transmission and reflectance spectrums are used to calculate the optical, electric and dielectric properties (i.e. the refractive index, extinction coefficient, optical and electrical conductivity), for KDPTGS crystals. Extinction coefficient k, refractive index n and the (realε, imaginaryε) parts of dielectric constant decrease with the increase of KDP concentration for KDPTGS crystals. The wavelength dispersion behavior of grown crystals has been revealed that the average single oscillator energy for electronic transitions (E_{so}) and dispersion energy or oscillator strength (E_{d}) of optical transitions and their values are found to be strongly dependent on the KDP ratio. The values obtained for the single-oscillator energy E_{so} are nearly consistent with the optical gap results. The optical conductivity increased with increasing photon energy. The optical transparency of KDPTGS crystals increased over the entire recorded UV-VIS-NIR spectrum. The enhanced optical transparency and band-gap envisage the suitability of the grown crystals for SHG applications.

References

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Figures Used

Fig. 1. Spectral distribution of normal incidence of (a) Transmittance $T(\lambda)$ and (b) Reflectance $R(\lambda)$ for KDPTGS single crystals.

Fig. 2. Plot of $(\alpha\hbar\omega)^{1/2}$ versus $h\omega$ for KDPTGS single crystals (inset plot of indirect optical energy gap $E_{g}^{\text{opt}}$ against KDP concentration).
Fig. 3. Spectral behavior of (a) refractive index $n$ and (b) extension coefficient $k$ for KDPTGS single crystals.
Fig. 4. Variation of the (a) real $\varepsilon_r$ and (b) imaginary $\varepsilon_i$ parts of the dielectric constant for KDPTGS single crystals.

Fig. 5. Spectra of the (a) real $\sigma_r$ and (b) imaginary $\sigma_i$ parts of the optical conductivity of KDPTGS single crystals.
Fig. 6. Relation between electric susceptibility $\chi_e$ as a function of photon energy $h\omega$ for KDPTGS single crystals.

Fig. 7. (a) The relation between $\left(\frac{1}{n^2} - 1\right)^{-1}$ and the squared photon energy $(h\omega)^2$ for KDPTGS single crystals. (b) $\left(\frac{1}{n^2} - 1\right)^{-1}$ and $(h\omega)^2$ fitted to the best straight line in the photon energy range $(h\omega = 4.6 - 7.2$eV).
Fig. 8(a): Variation of $(n^2 - 1)^{-1}$ versus $\lambda^2$ and $(n^2 - 1)^{-1}$ versus $\lambda^2$ fitted to the best straight line in the range $(0.2 - 2.4) \times 10^5$ (nm)$^{-2}$. 
Fig. 9. (a) The relation between $n^2$ and $\lambda^2$ (b) $n^2$ and $\lambda^2$ fitted to the best straight line in the range $(2-3) \times 10^{-5} \text{nm}^2$. 